

# Robust network design and its application to slicing

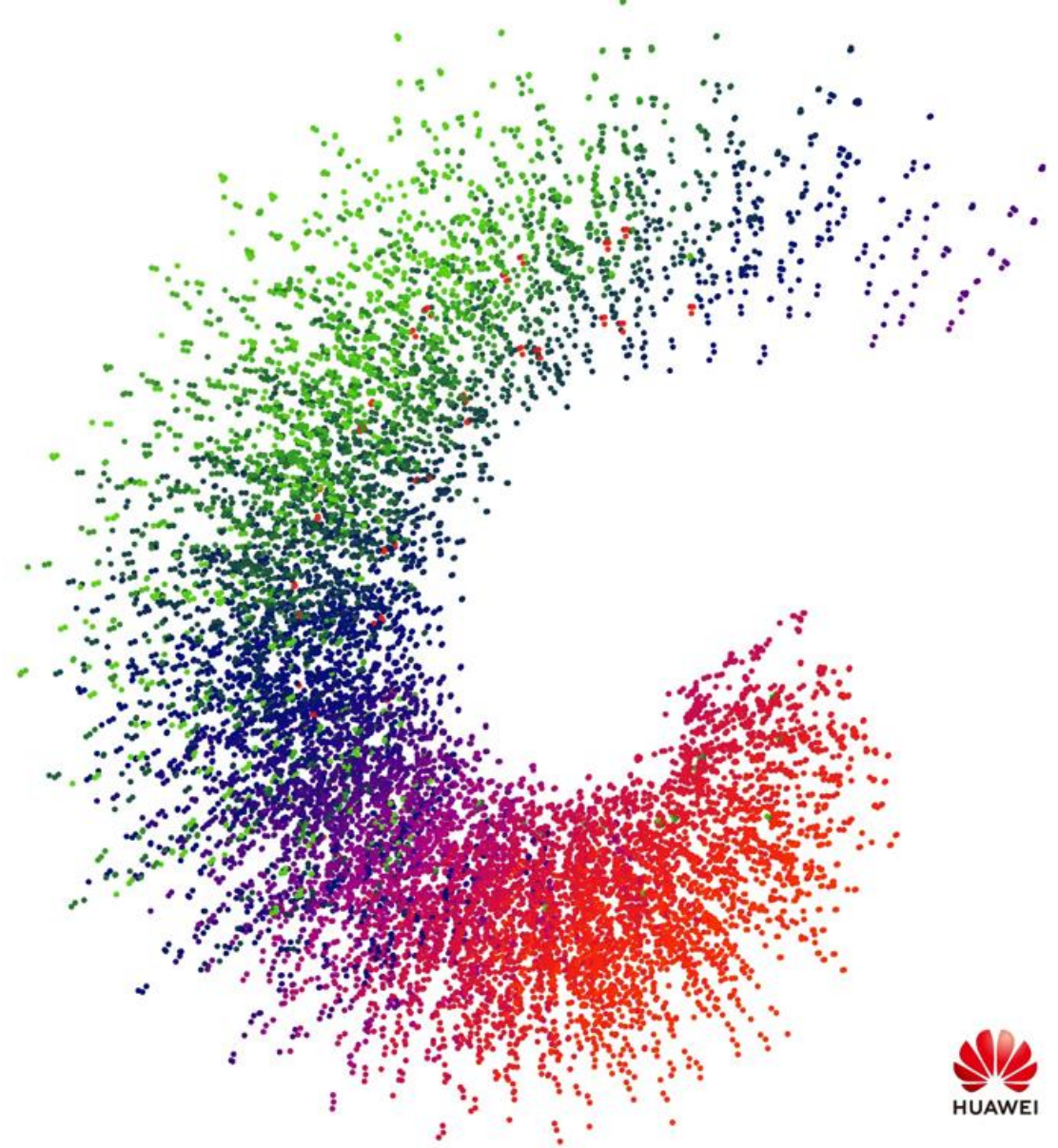
Julien Lesca

Senior researcher, Network OR, Datacom Dijkstra Lab



**Joint work with:**

Paolo Medagliani, Jérémie Leguay, Sebastien Martin, CaiShengming, Zengfeng, Yacine Al Najjar, Walid Ben Ameer



Agenda:

Slicing

Robust Design

Algorithm

Results

# Network Slicing Motivation: 5G and beyond

5G vision: enabling industry digitalization



Key requirements for 5G networks:  
differentiated network services

**Independent service operation**



Independent and visible services    Customized services    Independent upgrade    ...

**Secure isolation**



Smart grid    Industrial control    Autonomous driving    ...

**Guaranteed SLA**



Ultra-high bandwidth    Ultra-low delay    Massive connections    Ultra-high reliability    ...  
10 Gbit/s    < 1 ms    1 MB connection/km<sup>2</sup>    99.999%



eMBB



uRLLC



Massive IoT



RAN



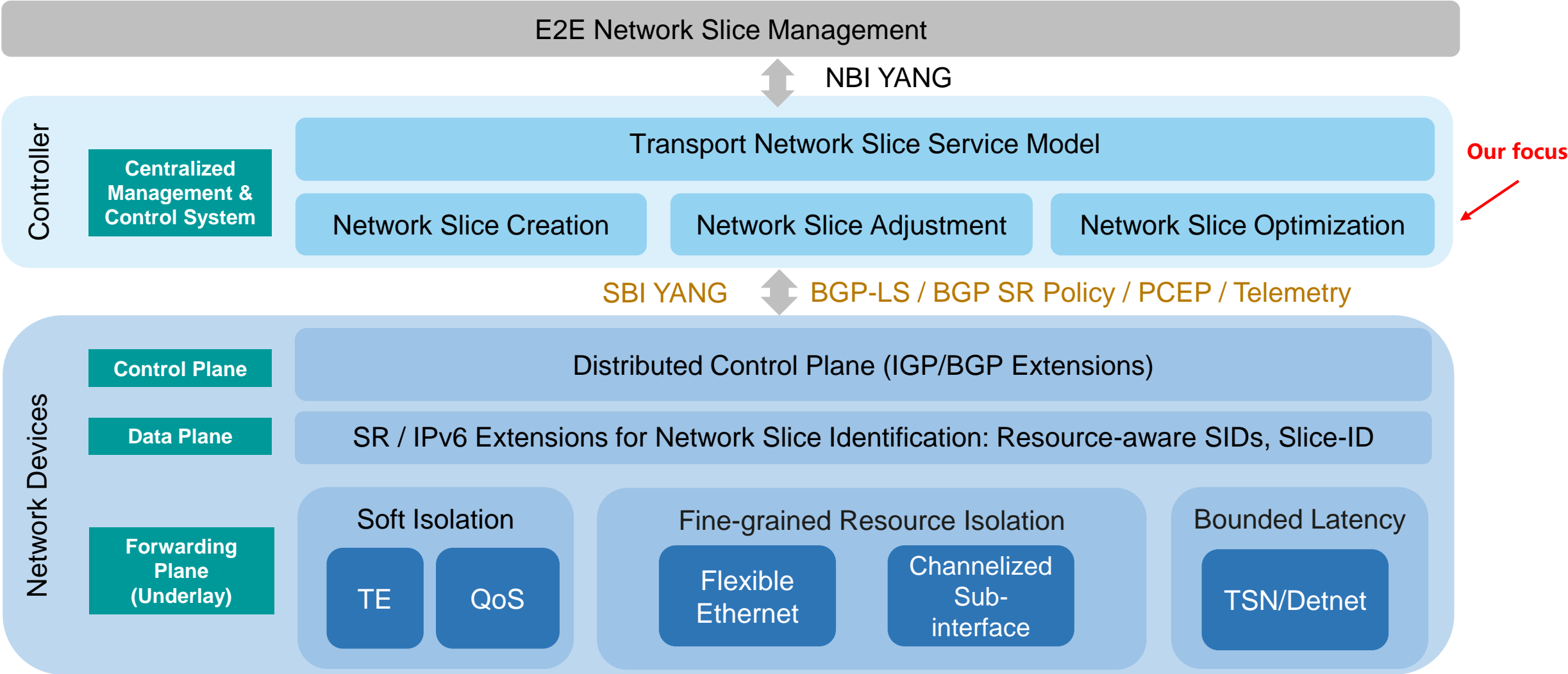
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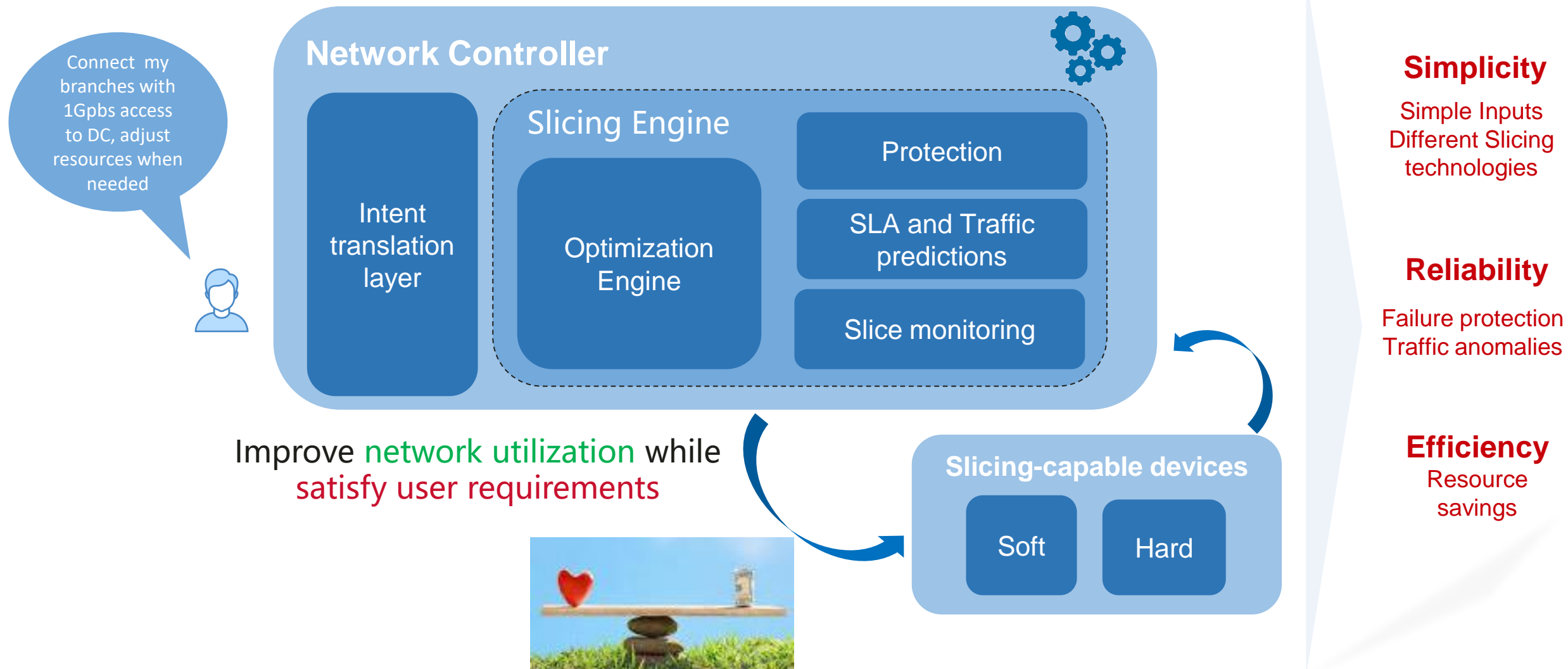
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**Slices = on-demand and end-to-end isolated networks**

# Network Slicing Architecture



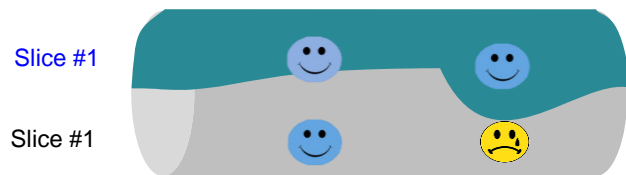
# Towards an Advanced Automation Slicing Engine



# Challenge #1: Allocate resources to meet SLA Requirements

## Isolation between slices

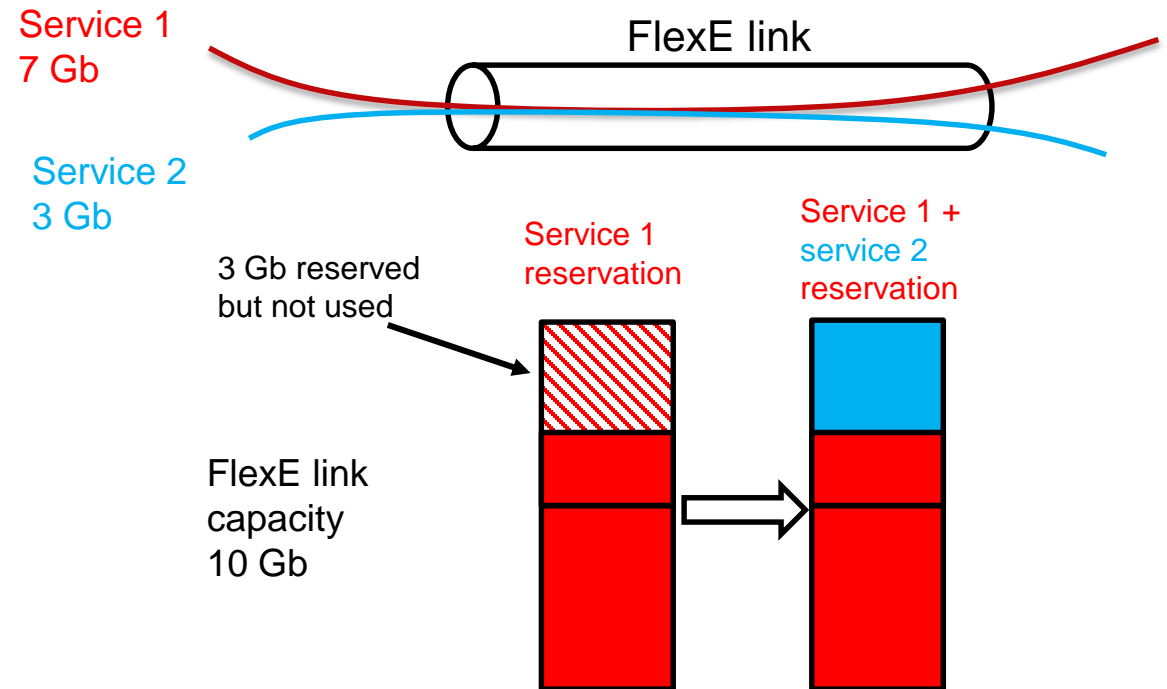
The traffic in one slice must not interfere with the performance of other slices



**Slicing technologies:** several technologies can be used to ensure isolation inside the data plane (FlexE, channelized sub-interfaces, HQoS)

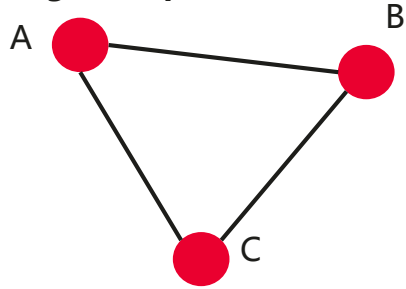
## Bandwidth reservation

**Bandwidth reservations in FlexE:** capacity slots are allocated with a granularity of 5GB (the 5 first slots are of 1GB)



# Challenge #2: Consider various Traffic Models - “Pipes” / “Hoses”

Running example:



Morning

	A	B	C
A		5	10
B	5		1
C	10	1	

Noon

	A	B	C
A		20	5
B	20		1
C	5	1	

Afternoon

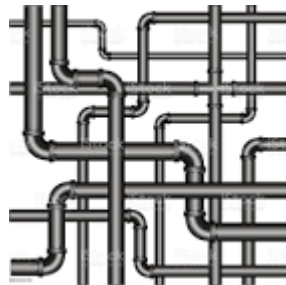
	A	B	C
A		10	1
B	10		10
C	1	10	

Per-Service (« Pipe » model with OD tunnels)

Per-Access Point (“VPN/Hose” model)

Aggregated « Pipe » model  
(Maximum traffic over the day)

	A	B	C
A		20	10
B	20		10
C	10	10	



« VPN/Hose » model  
(Access bandwidth for sites)

	Hose
A	25
B	21
C	11



Focus of this talk

Benefits:

Sometimes, traffic information is only available per access site. It is also easier to define by users and it “compresses” inputs. Users don’t want to over-specify.

Main challenge: **guarantee “non-blocking” slices** (ensure that 100% of traffic matrices can be routed)

⇒ **we need to solve a robust network design problem**

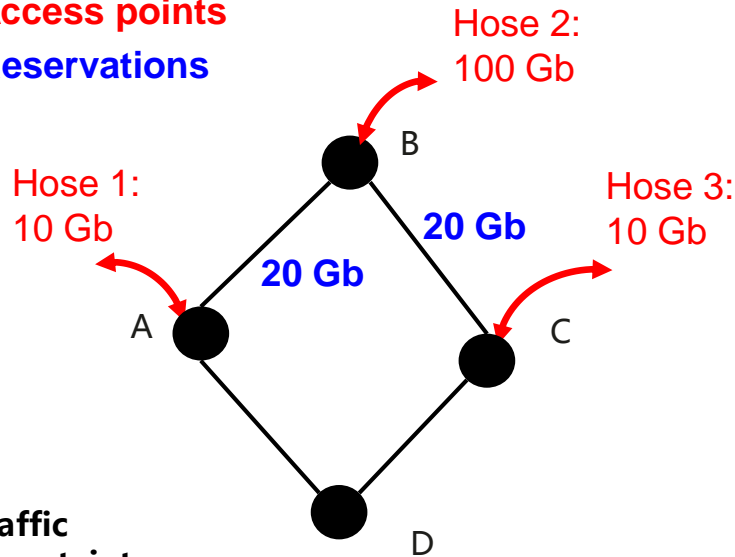
Note: Traditional business VPNs do not have such guarantee today.

# Possible specifications of traffic with Hoses

## All-to-all directions

Access points

Reservations



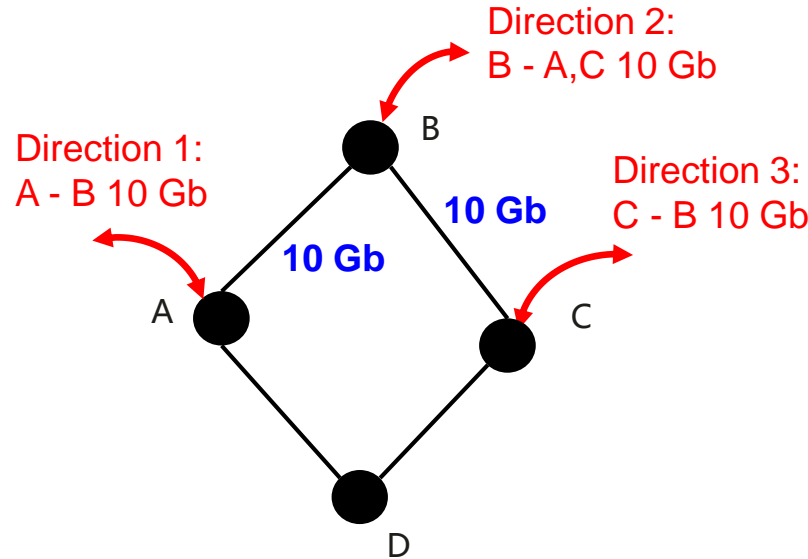
Traffic uncertainty:

Demand vector set  $D$  is a polytope described by inequalities

$$\begin{cases} d_{(A,B)} + d_{(A,C)} \leq 10 \text{ GB} \\ d_{(C,B)} + d_{(C,A)} \leq 10 \text{ GB} \\ d_{(B,A)} + d_{(B,C)} \leq 100 \text{ GB} \end{cases}$$

Traffic can go in all directions  
 ⇒ **costly in terms of reservations**

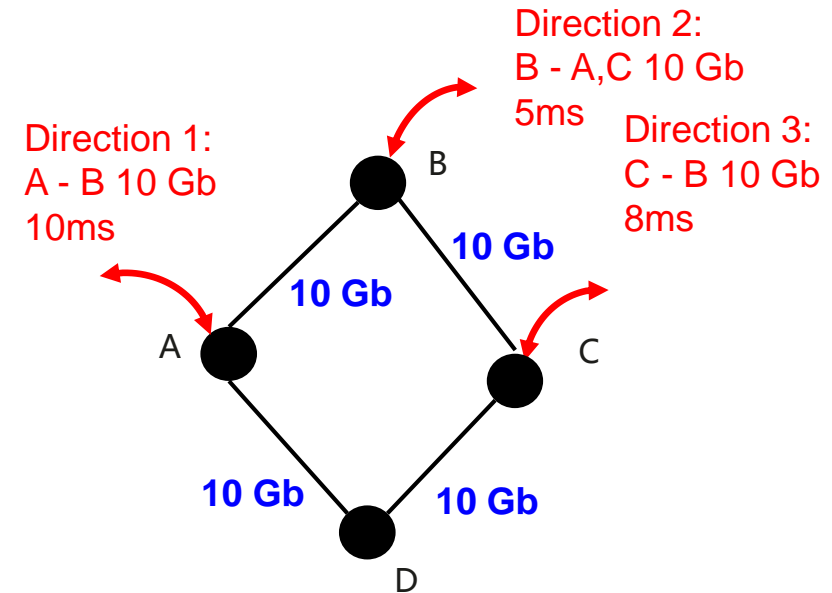
## Specific directions



$$\begin{cases} d_{(A,B)} \leq 10 \text{ GB} \\ d_{(C,B)} \leq 10 \text{ GB} \\ d_{(B,A)} + d_{(B,C)} \leq 100 \text{ GB} \end{cases}$$

Some directions may not be necessary  
 ⇒ **specify them to better utilize capacity**

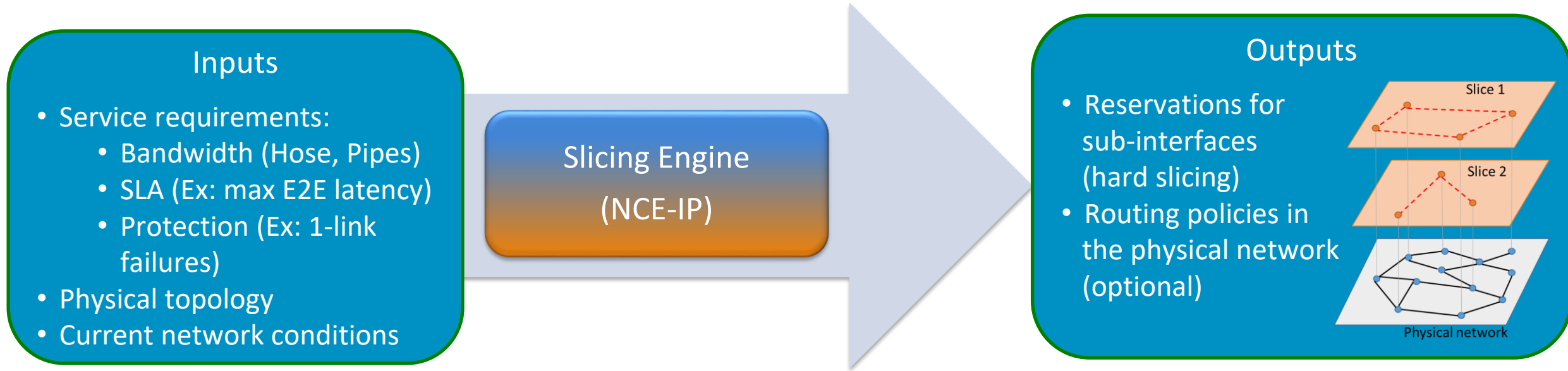
## Directions + QoS



$$\begin{cases} d_{(A,B)} \leq 10 \text{ GB} \\ d_{(C,B)} \leq 10 \text{ GB} \\ d_{(B,A)} + d_{(B,C)} \leq 100 \text{ GB} \end{cases}$$

Applications care about end-to-end QoS  
 ⇒ **add routing constraints to directions**

# Challenge #3: Optimize at large-scale



## Optimization intents

- Maximize traffic acceptance
- Minimize the reserved capacity
- Load balance link utilization
- ...

## Optimization challenges

- Handle large-scale networks (50k nodes in IPRAN)
- Get good solutions in a fast manner

## Optimization tools

- Use advanced math-heuristics based on combinatorial optimization to solve difficult path computation and resource allocation problems



# Robust network design:

## Minimum cost problem

- Input: cost vector  $\lambda \in \mathbb{R}_+^E$
- Decisions: capacities  $x \in \mathbb{R}_+^E$  such that there is a routing scheme that can route all demands  $d \in \mathcal{D}$  without exceeding the capacities (i.e. with a congestion  $\leq 1$ ), we denote the set of feasible capacities:
  - $X_{dyn}$  for a dynamic routing
  - $X_{sta}$  for a static routing
- The minimum costs problems for static and dynamic routing are:
  - $lin_{dyn} = \min_{x \in X_{dyn}} \sum_{e \in E} \lambda_e x_e$
  - $lin_{sta} = \min_{x \in X_{sta}} \sum_{e \in E} \lambda_e x_e$

# Robust network design variants: Example for Dynamic routing

## Minimum cost problem

- Input costs of 1 on all edges:  
 $\lambda_{e_1} = \lambda_{e_2} = 1, \lambda_{e_3} = \lambda_{e_4} = 0$
- Input demand polytope  $\mathcal{D}$

$$d_{h_1} + d_{h_2} \leq 1$$

$$d_{h_3} \leq 1$$

$$d_h \geq 0, \forall h \in \mathcal{H}$$

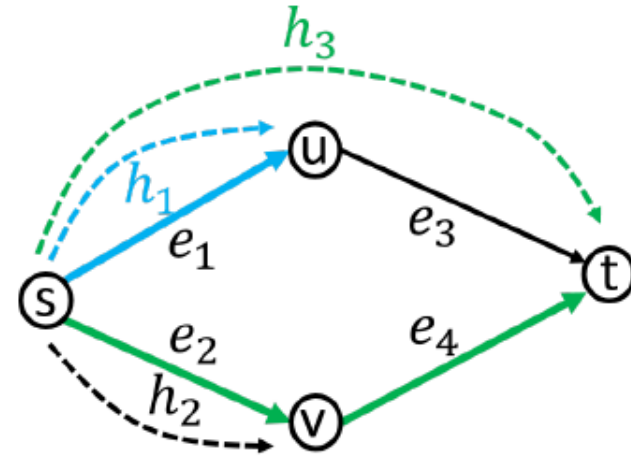
- $lin_{dyn}(\mathcal{D}) = 2$

Scenario:

$$d_{h_1} = 1$$

$$d_{h_2} = 0$$

$$d_{h_3} = 1$$

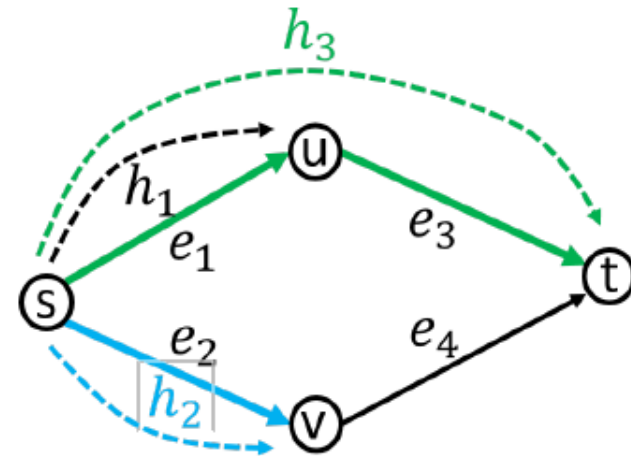


Scenario:

$$d_{h_1} = 0$$

$$d_{h_2} = 1$$

$$d_{h_3} = 1$$



# Robust network design variants: Example for Static routing

## Minimum cost problem

- Input costs of 1 on all edges:  
 $\lambda_{e_1} = \lambda_{e_2} = 1, \lambda_{e_3} = \lambda_{e_4} = 0$
- Input demand polytope  $\mathcal{D}$

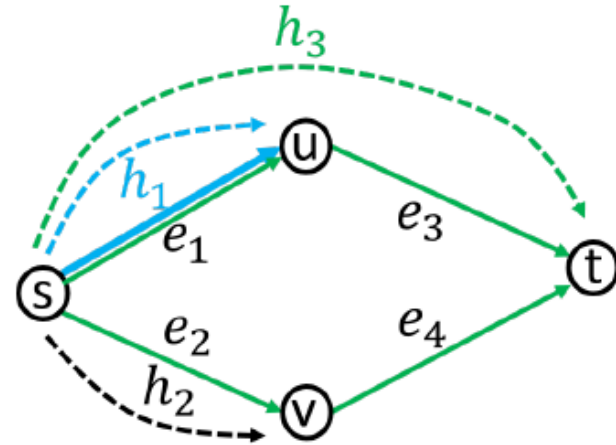
$$\begin{aligned} d_{h_1} + d_{h_2} &\leq 1 \\ d_{h_3} &\leq 1 \\ d_h &\geq 0, \forall h \in \mathcal{H} \end{aligned}$$

- The optimal static solution is to route half the demand  $h_3$  on the path  $(e_1, e_3)$  and the other half on the path  $(e_2, e_4)$ .

- $lin_{sta}(\mathcal{D}) = 3$

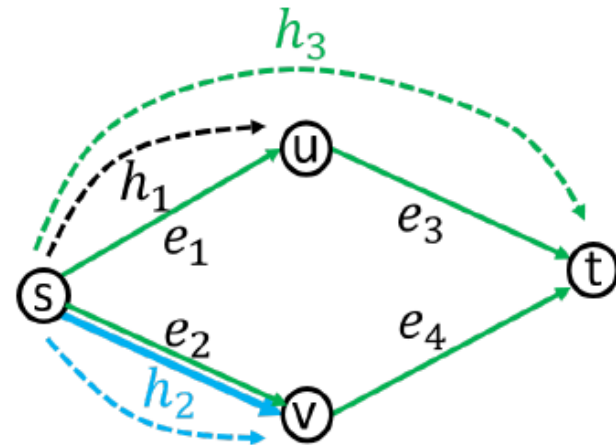
Scenario:

$$\begin{aligned} d_{h_1} &= 1 \\ d_{h_2} &= 0 \\ d_{h_3} &= 1 \end{aligned}$$



Scenario:

$$\begin{aligned} d_{h_1} &= 0 \\ d_{h_2} &= 1 \\ d_{h_3} &= 1 \end{aligned}$$



# Robust network design: Complexity results

- **Dynamic routing**

- Splittable case (Fractional routing)
  - CoNP-hard for directed graph (*Hardness of Robust Network Design, Chekuri, Shepherd, Oriolo and Scutellá, 2007*)

- **Static routing**

- Splittable case (Fractional routing)
  - Polynomial time solvable (*Routing of Uncertain Traffic Demands, Ben-Ameur and Kerivin, 2005*)
- Unsplittable case (Single path routing)
  - Without capacity: polynomial time solvable (*The VPN Conjecture Is True, Goyal, Olver and Sheperd, 2013*)
  - With capacity: NP-hard (*Provisioning a Virtual Private Network: A Network Design Problem for Multicommodity Flow, Gupta, Kleinberg, Kumar, Rastogi and Yener, 2001*)

# Robust slicing model

- Graph  $G = (V, E)$
- Access points  $Q \subseteq V$
- Ingress/egress bandwidth  $m_v^{in}, m_v^{out}$  for each access point  $v$
- Convergence ratio  $\mu_e$  for each edge  $e \in E$
- Bandwidth  $c_e$  of edge  $e \in E$
- Size configuration  $s_i^e$  on edge  $e \in E$
- Demands
  - $\mathcal{H}$  : pairs of access points able to communicate
  - $\mathcal{D}$ : possible demands for  $\mathcal{H}$ 
    - Subset of  $\{d \in \mathbb{R}^{\mathcal{H}} : \forall v \in V, \sum_{(v,u) \in \mathcal{H}} d_{(v,u)} \leq$

$$\min \sum_{e \in E} \sum_i \lambda^e s_i^e x_i^e$$

$$\left\{ \begin{array}{l} \sum_{p \in P_h} \varphi_h^p \geq 1, \forall h \in \mathcal{H} \quad \text{Flow constraint} \\ \mu_e \sum_{h \in \mathcal{H}} \sum_{p \in P_h: e \in p} d_h \varphi_h^p \leq \sum_i s_i^e x_i^e, \forall e \in E, \forall d \in \mathcal{D} \quad \text{Slot reservation constraint} \\ d_h^* \times \sum_{p \in P_h: e \in p} \varphi_h^p \leq \sum_i s_i^e x_i^e, \forall e \in E, \forall h \in \mathcal{H} \\ \sum_i s_i^e x_i^e \leq c_e, \forall e \in E \quad \text{Capacity constraints} \\ x_{i-1}^e \geq x_i^e, \forall e \in E, \forall i \end{array} \right.$$

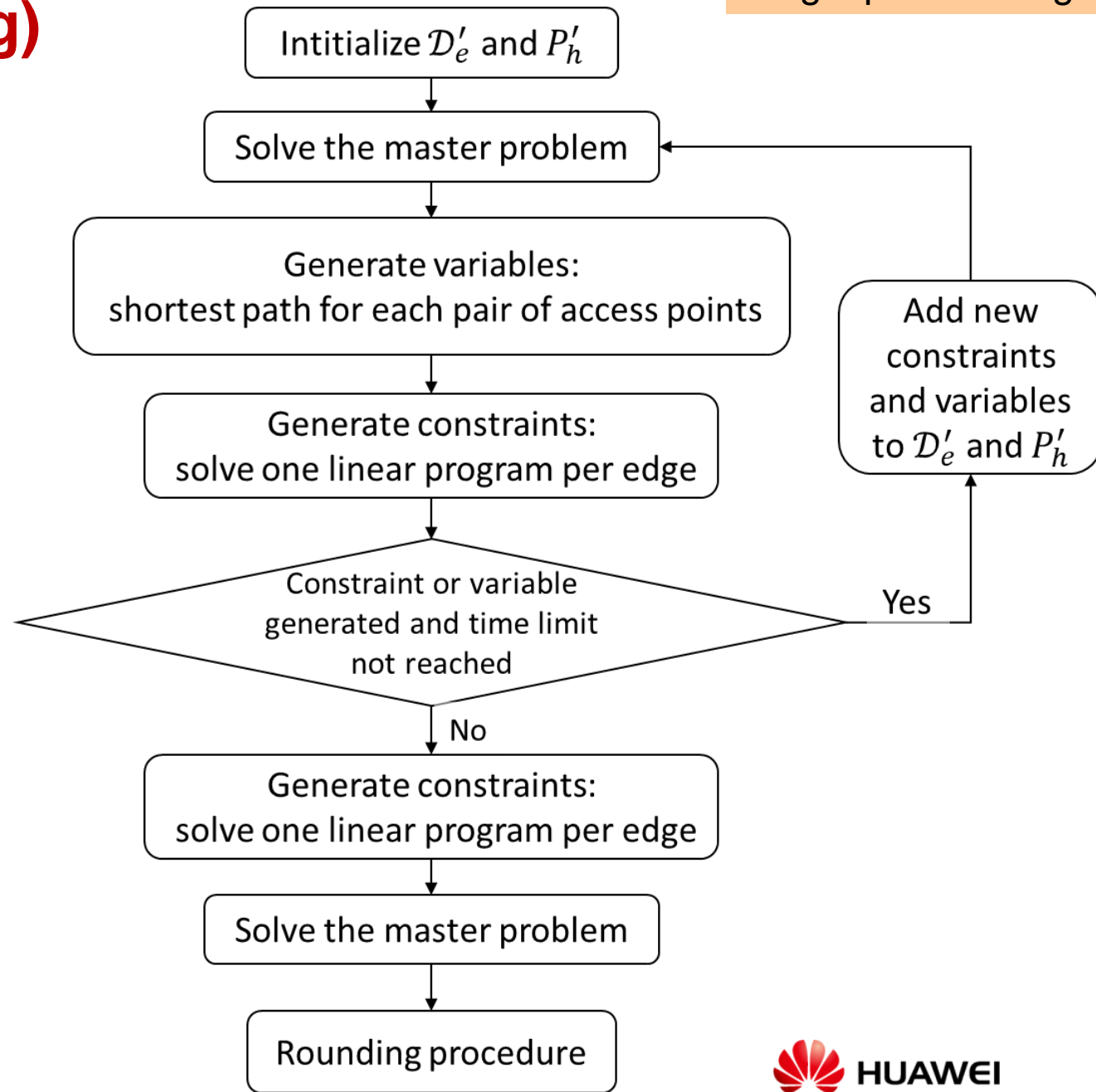
**Remark:** extended formulation with exponential number of paths and infinite demand constraints

$$d_h^* = \operatorname{argmax}_{d \in \mathcal{D}} d_h$$

# Solving algorithm (static routing)

## Master problem

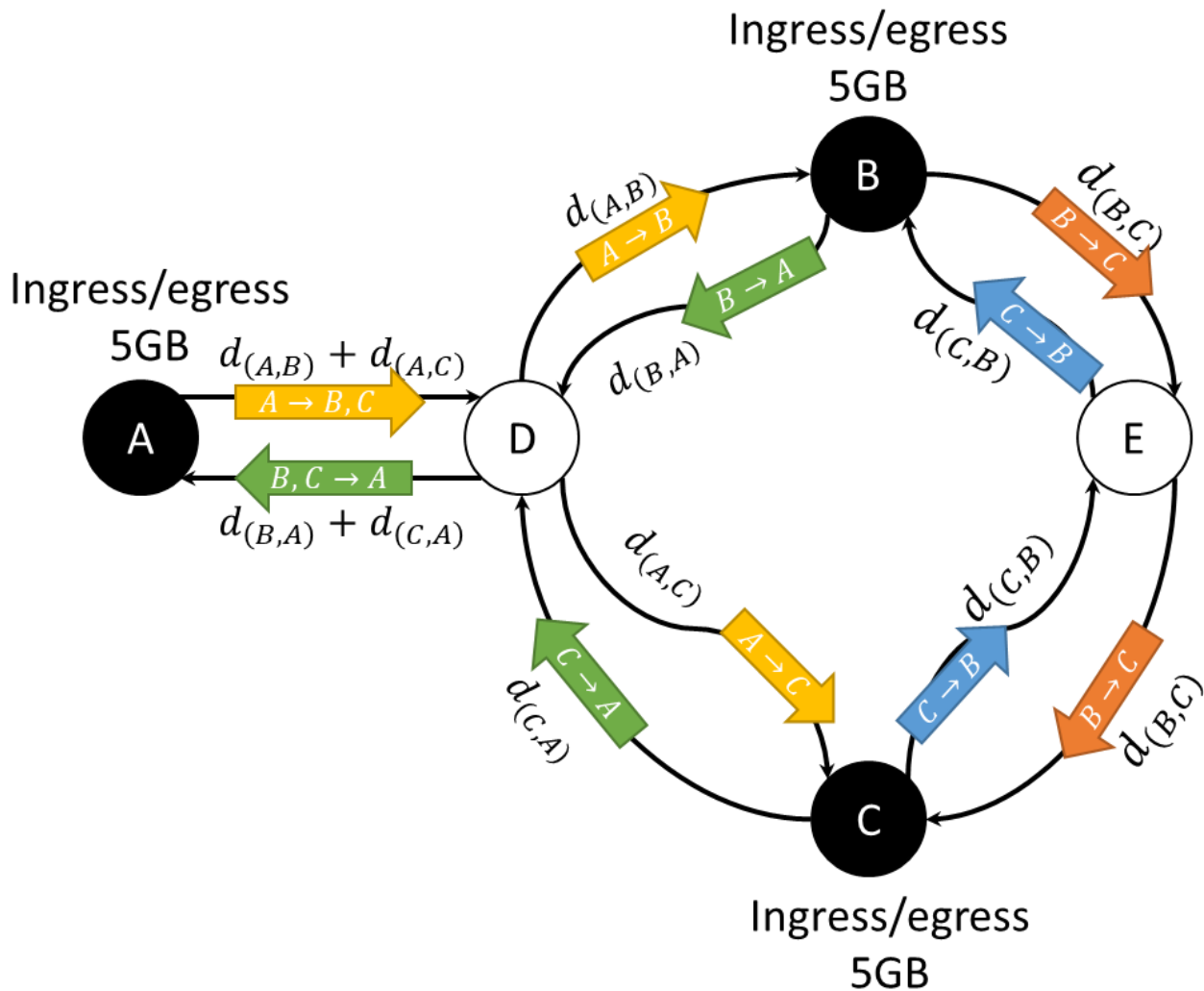
$$\begin{aligned}
 & \min \sum_{e \in E} \sum_i s_i^e x_i^e \\
 & \left\{ \begin{aligned}
 & \sum_{p \in P'_h} \varphi_h^p \geq 1, \forall h \in \mathcal{H} \\
 & \mu_e \sum_{h \in \mathcal{H}} \sum_{p \in P'_h: e \in p} d_h \varphi_h^p \leq \sum_i s_i^e x_i^e, \forall e \in E, \forall d \in \mathcal{D}'_e \\
 & \sum_i s_i^e x_i^e \leq c_e, \forall e \in E \\
 & x_{i-1}^e \geq x_i^e, \forall e \in E, \forall i
 \end{aligned} \right.
 \end{aligned}$$



# Illustrating example for the capacity design

$$\max \sum_{h \in H_e} d_h$$

$$H_e: \text{ set of demands that traverse edge } e \begin{cases} \sum_{(q,t) \in \mathcal{H}} d_{(q,t)} \leq m_q^{out}, q \in Q \\ \sum_{(s,q) \in \mathcal{H}} d_{(s,q)} \leq m_q^{in}, q \in Q \end{cases}$$



Capacity for edge (A, D)

$$\begin{matrix} \text{A egress} \\ \text{constraint} \end{matrix} \left\{ \begin{array}{l} \text{Max } d_{(A,B)} + d_{(A,C)} \\ d_{(A,B)} + d_{(A,C)} \leq 5GB \\ \dots \end{array} \right. = 5GB$$

Capacity for edge (B, E)

$$\begin{matrix} \text{B egress} \\ \text{constraint} \\ \text{C ingress} \\ \text{constraint} \end{matrix} \left\{ \begin{array}{l} \text{Max } d_{(B,C)} \\ d_{(B,A)} + d_{(B,C)} \leq 5GB \\ d_{(A,C)} + d_{(B,C)} \leq 5GB \\ \dots \end{array} \right. = 5GB$$

# Results for IPRAN networks

## Network topologies

- Small: 90 nodes, 200 links, 30 hoses
- Middle: 5.5 nodes, 11k links, 100 hoses
- Large: 55k nodes, 120k links, 100 hoses (approximately 10000 demands)

Instances with FlexE, Channelized interfaces and mixed.

## Benchmarks

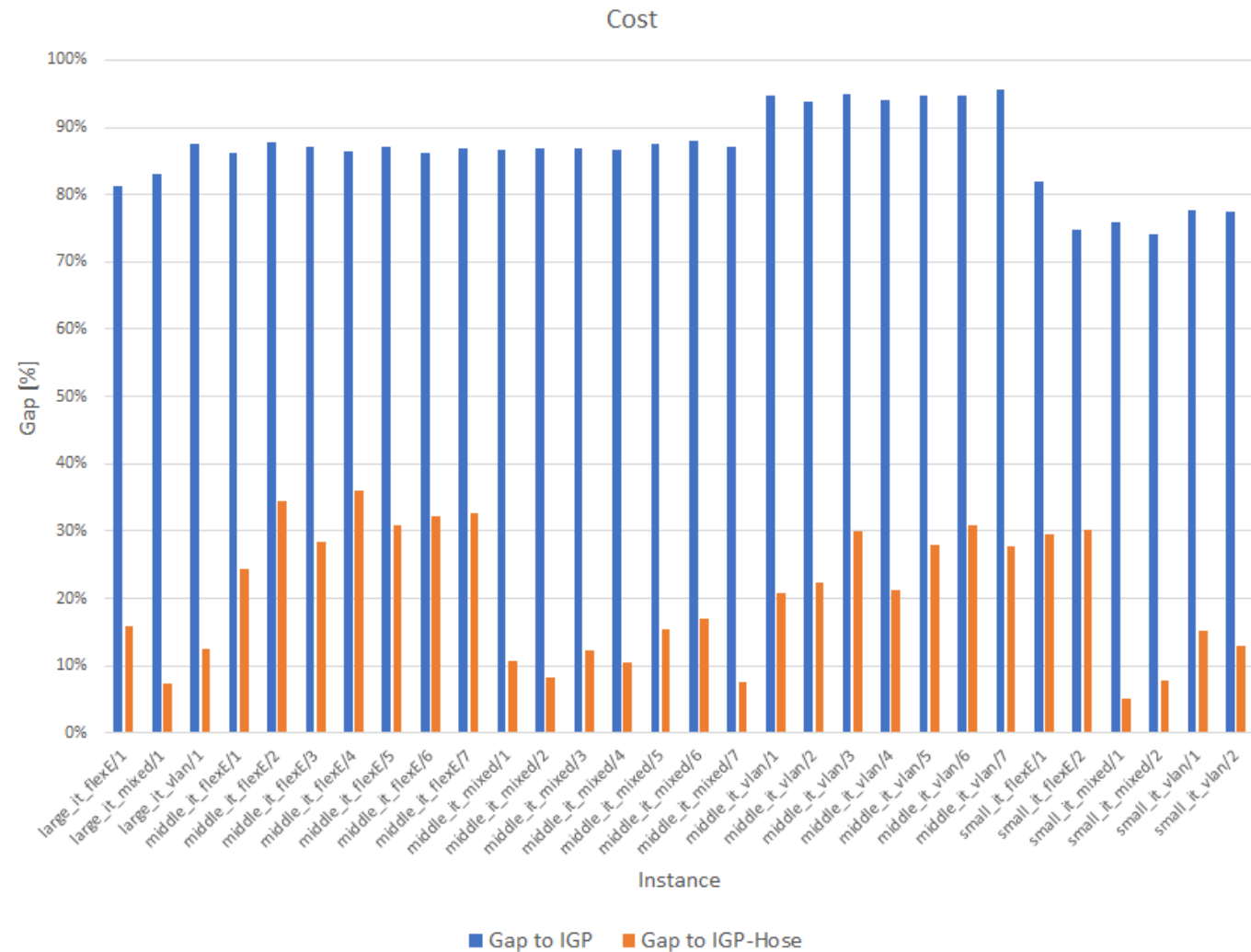
1. IGP shortest paths with worst case traffic in every directions (**IGP**)
2. IGP shortest paths with optimal reservations using the traffic polytope (**IGP-Hose**)

## Time limits

- Small: 30s
- Middle & Large: 600s

Main results:

**21% average gain over IGP-Hose and 86% over IGP**





# Conclusions

## ■ Robust network slicing

- › Slicing with simplified traffic information (hoses) calls for advanced algorithms to guarantee TMs can be routed

## ■ Future challenges

### › Data-driven approaches

- » Optimize reservations based on traffic predictions (dimensioning of hoses, identify relevant directions)

### › Advanced scenarios

- » Multi-domain network slicing (different technologies & granularities)
- » Hierarchical network slicing

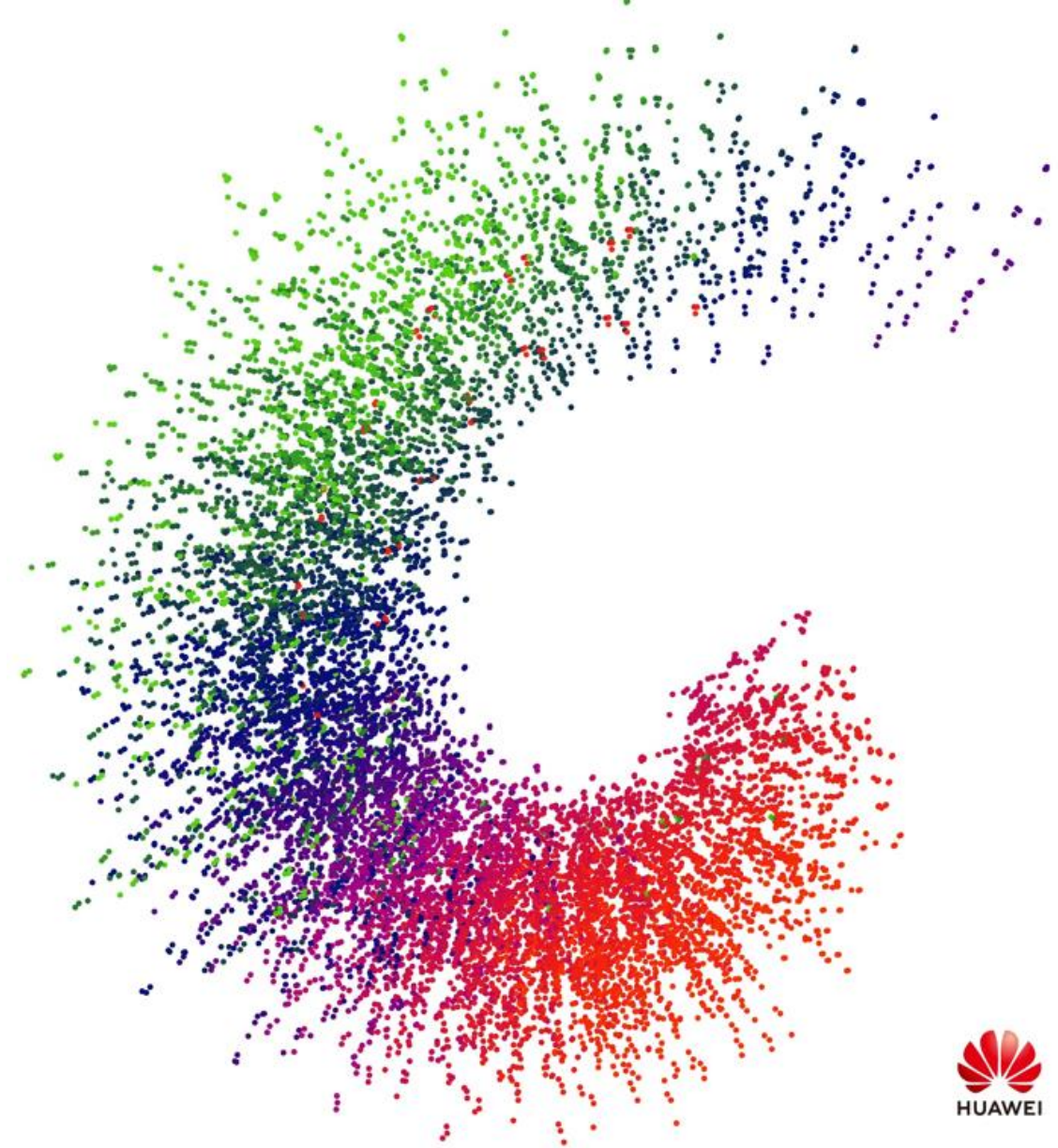
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# Thanks

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# Column & Constraint generation

## Pricing problem

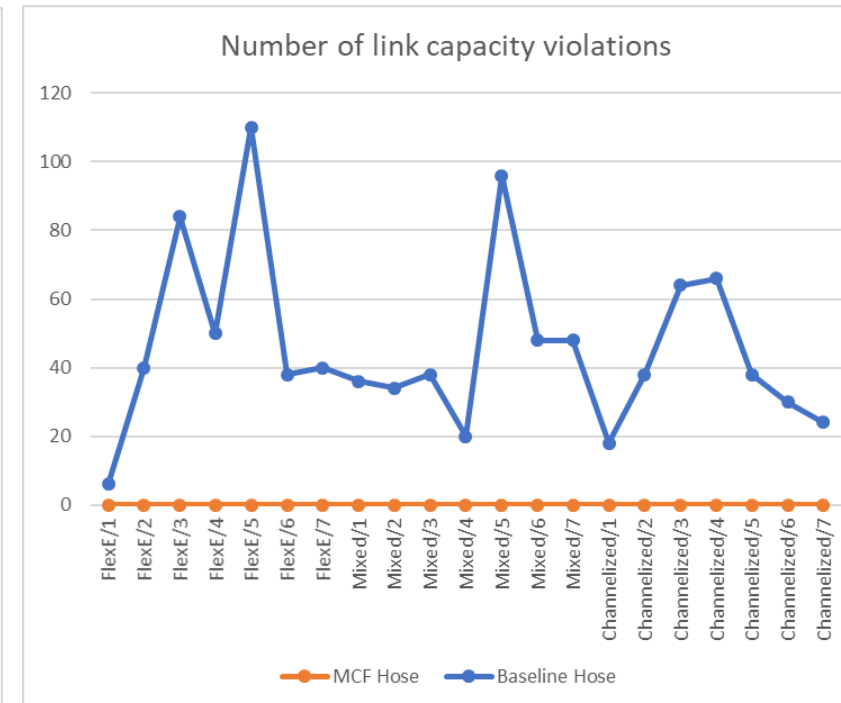
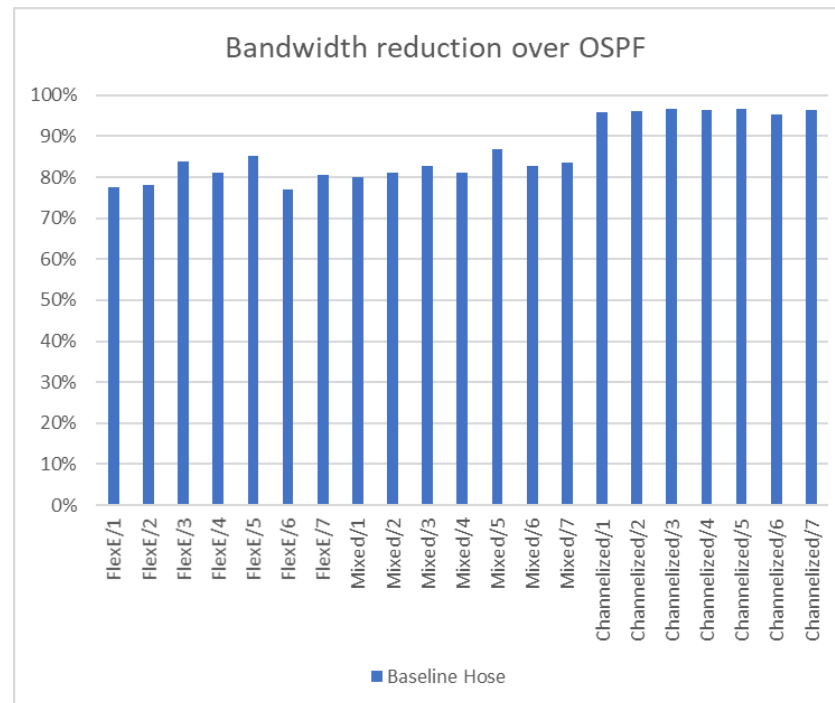
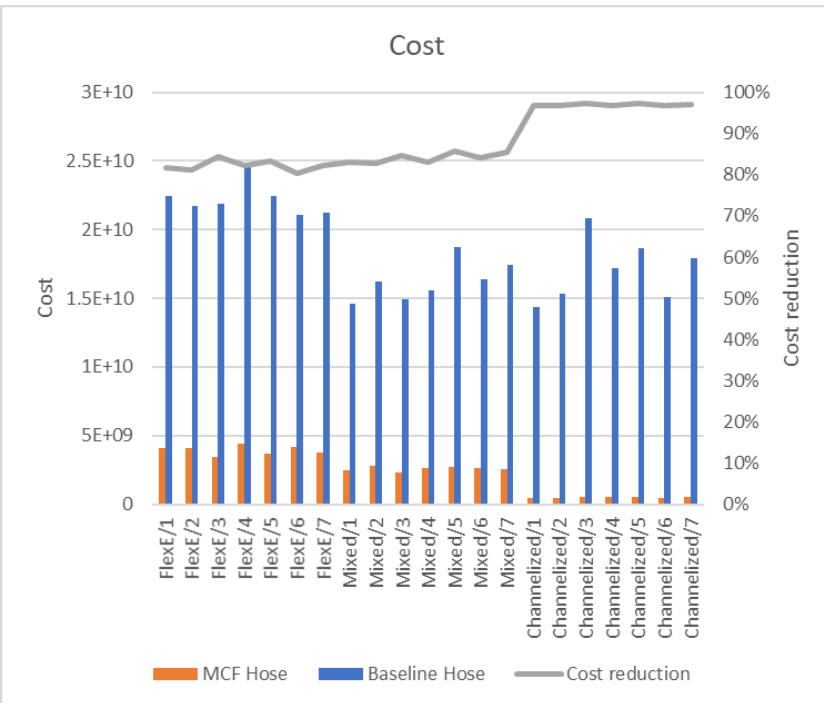
- Variables  $\varphi_h^p$
- $\alpha_h, \beta_d^e$  and  $\gamma_{d,h}^e$  simplex multipliers of the 1<sup>st</sup>, 2<sup>nd</sup> and 3<sup>rd</sup> constraints
- For any  $h \in H$ , find path  $p^* \in P_h$  which minimizes  $\sum_{e \in p^*} [\gamma_h^e + \mu_e \sum_{d \in \mathcal{D}'} \beta_d^e]$ 
  - Compute shortest path on  $G$  where the cost on edge  $e$  is  $[\gamma_h^e + \mu_e \sum_{d \in \mathcal{D}'} \beta_d^e]$
  - If  $\sum_{e \in p^*} [\gamma_h^e + \mu_e \sum_{d \in \mathcal{D}'} \beta_d^e] \leq \alpha_h$  holds then add variable  $\varphi_h^{p^*}$

## Cutting problem

- Constraints  $\mu_e \sum_{h \in H} \sum_{p \in P_h: e \in p} d_h \varphi_h^p \leq \sum_i s_i^e x_i^e$
- Solve the following linear programs ( $\mathcal{D}$  is a set of linear constraints)
 
$$\max_{d \in \mathcal{D}} \sum_{h \in H} d_h \sum_{p \in P_h: e \in p} \varphi_h^p$$
- If  $\mu_e OPT_{LP} \leq \sum_i s_i^e x_i^e$  then add constraint  $\mu_e \sum_{h \in H} \sum_{p \in P_h: e \in p} d_h^* \varphi_h^p \leq \sum_i s_i^e x_i^e$ 

where  $d^* = \operatorname{argmax}_{d \in \mathcal{D}} \sum_{h \in H} d_h \sum_{p \in P_h: e \in p} \varphi_h^p$

# Results for IPRAN networks



## Network topology

5500 nodes

12000 links

100 hoses (approximately 10000 demands)

Baseline is OSPF routing

Reduction computed as  $\frac{OSPF - MCFHose}{OSPF}$

The cost improvement of MCFHose over OSPF is between 80% and 97%

The bandwidth reduction is between 77% and 97%

While MCFHose finds a solution for all the hoses, the baseline presents some capacity violations (between 6 and 110 violated links) as it cannot routing traffic matrices